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## Squeeze Film Dampers Operation, models and issues of interest

#### Luis San Andrés Mast-Childs Chair Professor





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### Most common problems in rotordynamics

#### **<u>1. Excessive steady state synchronous vibration levels:</u>**

Improve balancing.

Modify rotor-bearing systems: tune system critical speeds out of RPM operating range.

Introduce damping to limit peak amplitudes at critical speeds that must be traversed.

#### **2. Subharmonic rotor instabilities**

Eliminate instability mechanism, i.e. change bearing design if oil whip is present.

Rise natural frequency of rotor system as much as possible.

Introduce damping to raise onset rotor speed above the operating speed range.

## **SFD Operation**



In a SFD, the journal whirls but does not spin. The lubricant film is squeezed due to rotor motions, and fluid film (damping) forces are generated as a function of the journal velocity.



SFD with squirrel cage

Shaft mounted on ball bearings whose outer race cannot rotate (only whirl) with either a squirrel cage (US), or a dowel pin (UK).

## SFD dynamic forced performance

depends on a) Geometry (L, D, c) b) Lubricant (density, viscosity) c) Supply pressure and through flow conditions (grooves) d) Sealing devices e) Operating speed (frequency) & journal **kinematics** 



Flow regimes: (laminar, superlaminar, turbulent)
Type of lubricant cavitation: gaseous or vapor air ingestion & entrapment

#### **Brief history of SFDs**

#### Parsons (1889)

Discloses first use of a SFD as a part of the first modern-day steam turbine.



**Cooper (1963)** 

Rolls Royce engineer investigates experimentally the performance of rotating machinery with a SFD.

In 1970s, SFDs become essential components in aircraft engines and multistage high pressure centrifugal compressors.



#### **Brief history of SFD (Turbomachinery Symposium)**

#### Zeidan et al. (1996)

History SFDs since 1960's and discuss major technical issues for their integration into turbomachinery, including oil cavitation vs. air ingestion and fluid inertia effects.

#### Kuzdal and Hustak (1996)

Tested various damper configurations (open and sealed ends) → optimized SFD reduces rotor synchronous motion amplitudes and raises stability threshold of a rotor bearing system.



## Other relevant past work

• Della Pietra and Adilleta (2002): Comprehensive review of research conducted on SFDs over last 40 years.

**Parameter identification in SFDs:** 

• **Tiwari et al. (2004):** Comprehensive review of parameter identification in fluid film bearings.

## (2006-2010) San Andrés and Delgado (SFD & MECHANICAL SEAL, improved predictive models).

GT 2006-91238, GT 2007-24736, GT 2008-50528, GT 2009-50175

(2012-2021) San Andrés and students (sealed ends SFDs for aircraft)

GT 2012-68212, GT 2013-94273, GT 2014-26413, GT 20015-43096, GT 2016-43096, GT 2016-56695, 2016 A/TPS, GT2018-76224, GT 2019-90330, GT 2021-58627

## **SFD** applications

#### Jet engines with rolling element bearings:

- a) To reduce synchronous peak amplitudes,
- b) Limit peak amplitudes at critical speeds,
- c) To isolate structural components (lower transmissibility), and
- d) To provide a margin of safety for blade loss.

#### Light hydrocarbon compressors with instability problems

- a) To stabilize unit by introducing damping and reducing crosscoupled effect of seals, hydrodynamic bearings, etc.
- b) To enhance limited damping available from tilting pad bearings.

#### Other benefits of SFDs on rotordynamic performance are:

- Tolerance to larger rotor motions
- Reduced balancing requirements

- \* Simpler alignment
- \* Less mount fatigue

## Intershaft dampers





Schematic view of an intershaft SFD

In multi-spool jet engines, intershaft dampers locate at the interfaces between rotating shafts

Intershaft dampers whirl motions (precessional and spinning) result from the combined imbalance responses of both LP and HP rotors.

## Types of end seals for SFDs

#### Reduce thru flow and increase damping. Most seal types cannot prevent air ingestion



Industry uses O-rings, while jet engines use piston rings.

#### **O-ring issues:**

Low weight (replace squirrel cage), Special groove machining, Material compatibility

#### Piston ring issues:

Cocking and locking Splits – leak too much

Design is highly empirical, except for end plate seals

## SFD feed groove and exit grooves





SFD with feed groove

SFD with end grooves and seals

<u>Too shallow grooves</u>: increase damping  $(d_g/c) < 10$ 

**Too deep grooves**: increase added mass  $(d_g/c)>10$ 

#### Feed holes with small

diameter ( high flow) resistance or with check valves prevent back flow and distortions in dynamic film pressures

# Feed & discharge grooves

Interact with film flow, develop large dynamic film pressures, Induce inertia force coefficients even in small clearance (c) SFDs

## Fundamental design consideration

The amount of damping (needed) is the critical design consideration.

**If damping is too large** the SFD acts as a rigid constraint to the rotor-bearing system with large forces transmitted to the supporting structure.

**If damping is too low**, the damper is ineffective and likely to permit large amplitude vibratory motion at synchronous and sub harmonic frequencies.

#### What is too large damping? What is too low?

# What is the effect of viscous damping on the dynamic response of a mechanical system?



#### Simple spring-damper-mass system



System response defined by natural frequency  $(f_n)$  & damping ratio  $(\zeta)$ 

$$f_n = 2\pi \sqrt{\frac{K}{M}}; \ \zeta = \frac{C}{2\sqrt{KM}}$$

Response amplitude |X/u|



#### Transmissibility (to ground)



- Damping=0.25

**Damping** helps only when rotor traverses a critical speed (natural frequency= $f_n$ ) but increases force transmissibility for operation above 1.44  $f_n$ 

#### More complex K-C-M system : rotor on flexible supports



More complicated response. Damping helps only when traversing a critical speed (natural frequency= $f_{n1}$  and  $f_{n2}$ ) but increases force transmissibility. Excessive damping LOCKS supports and increases system response.

## SFDs – the bottom line



Too little damping may not be enough to reduce vibrations. Too much damping may lock damper & will degrade system performance.

SFDs must be designed with consideration of the whole rotor-bearing system.

Physical damping magnitude is not as important as the system damping ratio!

## SFD models for forced response

Damping is needed for safe passage through critical speeds and to provide or increase system stability. Thus, models for SFD forced response are:

**Imbalance response analysis:** *SFD* forces for circular centered whirl orbits.



## Rotordynamic eigenvalue & stability analysis:

SFD force coefficients for dynamic journal motions about a static (equilibrium) position.

#### Numerical nonlinear formulations for transient

response analysis of rotor-bearing response. Abused in academic studies; nowadays too common with fast PCs

## Journal bearing model: steady state



Pressure field is invariant with time and increases as film thickness decreases to a minimum.

## SFD model: journal motions off-centered



journal center displacements (x,y)

SFD reaction force for small amplitude motions about a static off centered journal position

$$-\begin{cases}F_{X}\\F_{Y}\end{cases}=\begin{bmatrix}C_{XX} & C_{XY}\\C_{YX} & C_{YY}\end{bmatrix}\begin{cases}\dot{x}\\\dot{y}\end{bmatrix}+\begin{bmatrix}M_{XX} & M_{XY}\\M_{XY} & M_{YY}\end{bmatrix}\begin{cases}\ddot{x}\\\ddot{y}\end{bmatrix}$$

C: damping, M: inertia force coefficients

#### **SFD force coefficients**

NL functions of static journal eccentricity es

#### SFD model: pure radial squeeze (plunging motion)

0;  $v_r = f(t)$  $a_r = 0; a_t=0$ 

Pressure field changes with time and increases as film decreases. Note pressure reversals.



## Kinetics of whirl (circular) orbits



Journal center velocity with radial & tangential (V<sub>r</sub>,V<sub>t</sub>) components, and also acceleration (a<sub>r</sub>, a<sub>t</sub>)

For circular centered orbits, amplitude *e* is constant and whirl frequency = *@*.

 $\frac{\text{Circular centered orbit}}{V_t = e \omega ; V_r = 0}$  $a_r = -e \omega^2; a_t = 0$ 

SFD reaction forces:

- $F_r = (C_{rt} v_t + M_{rr} a_r)$
- $F_t = (C_{tt} v_t + M_{tr} a_r)$

C: damping M: inertia coefficients

## SFD model: circular centered orbits



SFDs DO NOT have a stiffness Misnomer:  $K_{rr} = \omega C_{rt}$   $\frac{\text{Circular centered orbit}}{V_t = e \ \omega \ ; \ V_r = 0}$  $a_r = -e \ \omega^2; \ a_t = 0$  $\frac{\text{SFD reaction forces:}}{F_r = -(C_{rt} \ V_t + M_{rr} \ a_r)}$  $F_t = -(C_{tt} \ V_t + M_{tr} \ a_r)$ 

Pressure is invariant in rotating frame. *P* follows -d*h*/d*t* rather than *h* (film)

## SFD model: small amplitudes centered orbit



#### FULL FILM MODEL

Damping (C) & inertia (M) force coefficients by Reinhart & Lund (1975)

$$C_{XX} = C_{YY} = C_{tt} = 12\pi \frac{\mu R^3 L}{c^3} \left[ 1 - \frac{\tanh\left(\frac{L}{D}\right)}{\left(\frac{L}{D}\right)} \right]$$

$$M_{XX} = M_{YY} = M_{rr} = \pi \frac{\rho R^3 L}{c} \left[ 1 - \frac{\tanh\left(\frac{L}{D}\right)}{\left(\frac{L}{D}\right)} \right]$$

Damping ~  $(R/c)^3$ , Inertia ~  $R^3/c$ 





## SFD sealed vs open

#### FULL FILM MODEL

#### Open ends

$$C_{XX} = C_{YY} = C_{tt} = \frac{1}{2}\pi \frac{\mu D L^3}{c^3}$$

$$M_{XX} = M_{YY} = M_{rr} = \frac{\pi \rho D}{24} \left(\frac{L^3}{c}\right)$$

#### (fully) Sealed ends

$$C_{XX} = C_{YY} = C_{tt} = \pi \frac{12}{8} \frac{\mu D^3 L}{c^3}$$

$$M_{XX} = M_{YY} = M_{rr} = \pi \frac{\rho D^3 L}{8c}$$

Increase in damping (and inertia) is large! For (*L/D*)=0.2=1/5, increase is **25x3** fold

 $C_{tt} \frac{sealed}{open} = M_{rr} \frac{sealed}{open} = 3 \left(\frac{D}{L}\right)^2$ 



## SFD model: circular centered orbits



## Short length open ends SFD (Pl film model)

Y

$$C_{tt} = \frac{\pi \mu D}{4\left(1 - \varepsilon^2\right)^{3/2}} \left(\frac{L}{c}\right)^3; \ C_{rt} = \frac{\mu \varepsilon D}{\left(1 - \varepsilon^2\right)^2} \left(\frac{L}{c}\right)^3$$

$$M_{rr} = \frac{\pi \rho D}{24} \left(\frac{L^{3}}{c}\right) \left[1 - 2\left(1 - \varepsilon^{2}\right)^{\frac{1}{2}}\right] \left\{\frac{\left(1 - \varepsilon^{2}\right)^{\frac{1}{2}} - 1}{\varepsilon^{2}\left(1 - \varepsilon^{2}\right)^{\frac{1}{2}}}\right\};$$

$$M_{tr} = -\frac{27}{140\,\varepsilon}\,\rho\,D\left(\frac{L^3}{c}\right)\left[2 + \frac{1}{\varepsilon}\ln\left(\frac{1-\varepsilon}{1+\varepsilon}\right)\right]$$

Damping ~  $(L/c)^3$ , Inertia ~  $L^3/c$ 

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## SFD model: circular centered orbits



Short length open ends SFD  $\pi$  film model

$$F_r = - (C_{rt} v_t + M_{rr} a_r)$$

 $\mathbf{F}_{t} = - \left( \mathbf{C}_{tt} \mathbf{v}_{t} + \mathbf{M}_{tr} \mathbf{a}_{r} \right)$ 

Nonlinear force coefficients, Large damping, Large inertia for  $Re_s = \rho \omega^2 c/\mu > 10$ 

## Identification of SFD force coefficients for two SFDs: open ends & sealed ends

**Sponsor: Pratt & Whitney Engines** 

2008-2018

## SFD test rig



## Test rig photograph



## Lubricant flow path

#### ISO VG 2 oil



## **Multiple-year test program**

(2008-2018)



Objective: Optimize SFD influence on rotor dynamics.



## Identification of SFD force coefficients





## **Test procedure**

X Displacement [µm]



al

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#### (1) Apply loads $\rightarrow$ record BC motions

 $\mathbf{z}^{1} = \begin{bmatrix} x_{(t)}^{1} \\ y_{(t)}^{1} \end{bmatrix} = \begin{bmatrix} X^{1} \\ Y^{1} \end{bmatrix} e^{i\omega t}$  $\mathbf{z}^{2}$ 

Shakers apply forces  $\mathbf{F}^{1} = \operatorname{Re}\left(\begin{bmatrix} F_{X}^{1} \\ iF_{y}^{1} \end{bmatrix} e^{i\omega t}\right)$ 

**Record BC** 

displacements

and accelerations

$$\mathbf{F}^{2} = \operatorname{Re}\left(\begin{bmatrix} F_{X}^{2} \\ -iF_{Y}^{2} \end{bmatrix} e^{i\omega t}\right)$$

 $\mathbf{z}^{2} = \begin{bmatrix} x_{(t)}^{2} \\ y_{(t)}^{2} \end{bmatrix} = \begin{bmatrix} X^{2} \\ Y^{2} \end{bmatrix} e^{i\omega t}$ 

 $a^2$ Load **F**<sub>(*i*)</sub>, displacement **z**<sub>(*i*)</sub> and acceleration **a**<sub>(*i*)</sub> recorded at each frequency

**EOM: Frequency Domain** 

$$[\mathbf{K}_{\mathbf{L}} + i\omega\mathbf{C}_{\mathbf{L}} - \omega^{2}\mathbf{M}_{\mathbf{L}}]\overline{\mathbf{z}} = \overline{\mathbf{F}} - M_{BC}\overline{\mathbf{a}} \longrightarrow \mathbf{H}_{\mathbf{L}}\mathbf{z}$$



#### **Identification of parameters**

#### Step 2 : Transform to frequency domain and curve fit H<sub>L</sub>'s



Physical model  $\operatorname{Re}(H_{XX}) \rightarrow K - \omega^2 M$  and  $\operatorname{Im}(H_{XX}) \rightarrow C \omega$ agree well with experimental data. Damping C is constant over frequency range

SFD



**SFD coefficients** 

 $(K, C, M)_{SFD} = (K, C, M)_{L} - (K, C, M)_{S}$ 

Test system (lubricated)

Dry structure

#### GT2015-43096

## Force coefficients for two open ends SFDs

1 inch land (*L/D*=0.20) Clearance: *c*=small (5 mil) vs. large (10 mil)


#### SFD test bearing and film geometry



#### Normalization of force coefficients

Force coefficients normalized to magnitudes from classical formulas (prior slide):

$$\overrightarrow{C} = \frac{C}{C^*} \quad \overrightarrow{M} = \frac{M}{M^*}$$
Damper A  
 $C_A = 0.129 \text{ mm}$ 

$$C^*_A = 6.01 \text{ kN.s/m}, \quad M^*_A = 2.69 \text{ kg}$$

$$C^*_B = 0.95 \text{ kN.s/m}, \quad M^*_B = 1.37 \text{ kg}$$

 $\overline{C}$  ~1  $8\overline{M}$  ~1 denote <u>one to one</u> agreement with predictive formulas.

**Damper A** (
$$c_A = 129 \,\mu$$
m) – damping coeffs.



**Findings: Damping** coefficients **increase** with increasing **orbit amplitude** and **static** eccentricity. At  $r/c_A \le 0.2, \overline{C}_{A-XX} \sim 0.85$ .

#### **Damper A** ( $c_A = 129 \,\mu$ m) added mass coeffs.



Findings: Added mass coefficients increase with increasing static eccentricity; but decrease with increasing orbit amplitude. Theory under predicts inertia coefficient, even for small amplitude motions.

#### Compare damping coeffs. of two dampers





Damping coefficients for small film clearance ( $c_A$ ) damper are ~4 times larger than the coefficients obtained with larger clearance ( $c_B$ ) SFD.

#### **Compare inertia coeffs. of two dampers**





Added mass coefficients for the small film clearance  $(c_A)$ damper are ~1.8 times higher than the coefficients obtained with larger clearance  $(c_B)$  SFD.

#### From circular orbit tests

 Damper A
 Damper B

 c\_A=0.129 mm
 c\_B=0.254 mm

- (a) For both dampers, **direct damping** coefficients do not show + sensitivity to the size of the orbit radius (*r*).
- (b) Inertia coefficients for the large clearance damper B are insensitive to orbit amplitude (*r*), while small clearance damper A shows added masses decreasing with orbt size (*r*).

#### SFD force coefficients Comparison between short and long <u>open</u> <u>ends</u> dampers with a central groove



#### Generation of dynamic pressure in film and groove

**Does** a (deep) central groove isolate a damper into two independent halves?



#### Conventional knowledge: A groove has constant pressure

#### Generation of dynamic pressure in a groove



#### No! grooves produce squeeze film pressures!

#### **compare SFD damping**



Ratio of coefficients ~  $(L/c^3)$ 

#### Long and short SFDs (circular orbits)

#### **compare SFD inertia**



Ratio of coefficients ~ (L/c)

#### Long and short SFDs (circular orbits)

#### **Closure II:** Long vs short SFDs

- Open ends long damper shows ~ 7 times more damping than short length damper. Inertia coefficients are twice larger.
- SFD force coefficients are more a function of static eccentricity (max. 2 mil) than amplitude of whirl & changing little with ellipticity of orbit.
- For all damper configurations and most test conditions: cross-coupled damping and inertia force coefficients are small.

#### Experimental SFD force coefficients Comparison open ends & sealed ends long (1") SFD

#### Damper A ( $c_A$ =140 µm (5.5 mil))



#### **compare SFD damping**



#### **Open ends vs sealed ends (circular orbits)**

#### **compare SFD inertia**



#### **Open ends vs sealed ends (circular orbits)**

#### **Closure III: Open vs Sealed SFDS**

Sealed ends long damper has ~ 3 times more damping than <u>open ends damper</u>. Inertia coefficients are 1.5 times larger.

SFD force coefficients are more a function of static eccentricity (max. 50 micro-m) than of the amplitude of whirl. Coefficients change little with ellipticity of orbit (up to 5:1 ratio)

Proper installation of piston rings is crucial for adequate sealing.

## Oil cavitation OR air ingestion in SFDs?



#### **Cavitation in liquid bearings**



#### **Cavitation in oil lubricated bearings**

Pressure is uniform (constant) inside cavitation "bubble" – Flow reformation at trailing edge of bubble



But... air ingestion & entrainment persist under dynamic load conditions.

Classical cavitation models do not apply to air entrainment under dynamic loading.

#### **SFD Operation Issue**

#### Air ingestion and entrapment



Bubbly Iubricant exits from top and bottom ends of damper



#### **Onset of air ingestion**

#### **Sealed ends SFD**



Oil foamy mixture evolves from lubricant exiting through piston ring slit.

## After 10 years of continued work,

## what did we learn?

#### **Conclusion (1):**

- (a) Damping (C) and inertia (M) coefficients are ~ isotropic, i.e.,  $C_{XX}$ ~ $C_{YY}$  and  $M_{XX}$ ~ $M_{YY}$ . Cross-coupled coefficients are small for most whirl type motions.
- (b) Simple theory does a modest job in producing physically accurate results for test SFDs with feed groove.
- (c) SFDs generate large added mass coefficients, more so for sealed ends configurations and with (deep) feed and discharge grooves.

#### Conclusion (2):

(d) A sealed SFD produces significantly (3+X) more damping and ~twice the added mass than an open ends SFD.

(e)The amplitude and shape of whirl motion have small effect on the SFD force coefficients.

(f) Air ingestion impairs the growth of film pressures for increasing orbit amplitudes and frequency → damping coefficients decrease.

The experimental results demonstrate SFDs are mostly linear mechanical elements.

#### Modern SFDs

## Integral SFDs



#### A few pointers ...



#### ASME GT 2012-68564

#### Integral Squeeze Film Damper (ISFD)



No squirrel cage EDM manufacturing process produces separate arcuate damper film lands with S-shape flexural springs.

Advantages low number of parts - short axial span - light weight - higher tolerance precision.

#### **ISFDs:** the sum of experiments

**2011** Identification of Force Coefficients in a 5-pad Tilting Pad Bearing with an Integral Squeeze Film Damper (Delgado et al. at GE)

#### GT2012-68564 Rotordynamic

Characteristics of a Flexure Pivot Pad Bearing with an Active and Locked Integral Squeeze Film Damper (Agnew and Childs)



**2017** Dynamic Characterization of an Integral Squeeze Film Bearing Support Damperfor a Supercritical CO<sub>2</sub> Expander (Ertas et al. at GE)

### ISFD produces significant damping & inertia coefficients.





#### **ISFD tests in Delgado (2011)**



over-estimates inertia by 30%

#### Our aim

#### GT2020-14182

# End seals amplify viscous damping! Quantify the effect of various end seal gaps on the dynamic forced performance of an ISFD.

Tilting pad journal bearing

ISFD film land

S-Spring

> 2019: Conduct dynamic load tests on a dedicated test rig to obtain ISFD force coefficients for ready comparison and validation of the model.

#### **Test ISFD** $\rightarrow$ Load between pads



Diameter at film land,  $D_{ISFD}$ Length, LFilm clearance, cArc radius,  $\alpha$ End seals gap,  $b_1$ 

**ISO VG46** Viscosity,  $\mu$ Density,  $\rho$ Supply flow rate, Q 157 mm (6.18 in) 76 mm (3 in) 0.356 mm (14 mil) 73° - 4 pads 0.28 mm, 0.43 mm, 0.53 mm, open ends

31.2 cP (at 46 ⁰C) 860 kg/m<sup>3</sup> 9.5 L/min (set pressure)

#### End seals ISFD → Shimmed End Plates



#### End seals gap = shim thickness $b_1$

<i>b</i> <sub>1</sub> (mm)	c/b <sub>1</sub>
0.53	1.49
0.43	1.21
0.28	0.79



#### **Test Rig for Dynamic Load Experiments**



ITEM NO.	PART NO.
1	Test-rig pedestals
2	air turbine motor
4	Test rotor
5	Bearing stator
7	Collection Chambers
8	Static Loader Yoke
9	BedPlate
10	Pitch stabilizer bolts
11	Bellow Coupling
12	Torque meter (rotor)
13	Torque meter (stator)
14	Torque limiter

Max Speed:16 krpm Max Static Load: 22 kN Max Dynamic Load: 4.4 kN, 1 k Hz



#### **ISFD (lubricated) dynamic complex stiffness H**L



#### Stiffness vs. static eccentricity vs. gap in end seal



#### Damping vs. static eccentricity vs. gap in end seal



 $c=356 \,\mu\text{m}, e/c=0-0.7, 9-166 \,\text{Hz}, Q \sim 9.5 \,\text{L/min}, P_s=1 \sim 2 \,\text{barg}$ 

Ζ
#### Added mass vs. static eccentricity vs. gap in seal

#### (*M<sub>XX</sub>*, *M<sub>YY</sub>*) [kg]



Inertia coefficient (added mass) larger than bearing mass (19 kg)

feed hole  $D_1 I_2$   $(P_3)$   $P_4$   $P_4$  $P_1$   $P_2$   $P_4$   $P_4$ 

c=356 μm, e/c=0-0.7, 9-166 Hz, Q~9.5 L/min, P<sub>s</sub>=1 ~ 2 barg

### **Conclusion ISFDs**

- (a) ISFD does not produce a film direct stiffness  $K_{ISFD}$  except for the test condition with the tightest end seal.
- (b) Damping  $C_{ISFD}$  increases with static eccentricity (large static load) but not as pronounced as theory predicts.
- (c) Added mass  $M_{ISFD}$  increases as gap decreases but ISFD with tightest gap ( $b_1 = 0.28$  mm < c) produces a stiffening hardening (negative virtual mass).
- (d) End seals with small gap amplify  $C_{ISFD}$ . Configuration with gap  $b_1=0.28$  mm produces 22 more damping that the open ends ISFD.
- (e) For static eccentricity (e<0.4c), model with fluid compressibility predicts well the ISFD experimental damping coefficients but not its added mass.

## Acknowledgments

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#### Learn more:

http://rotorlab.tamu.edu

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